

1. ...

2. Leite ab nach t ab

$$\begin{aligned}\frac{d}{dt} \sin 2\omega t &= 2\omega \cos 2\omega t \\ \frac{d}{dt} \cos 2\omega \left(t - \frac{T}{2}\right) &= -2\omega \sin \omega (2t - T) \\ \frac{d}{dt} \cos 2\omega \left(t - \frac{T}{2}\right)^2 &= -4\omega t \left(\sin \frac{1}{2}\omega (2t - T)^2\right) + 2\omega T \left(\sin \frac{1}{2}\omega (2t - T)^2\right)\end{aligned}$$

$$\begin{aligned}\frac{d}{dt} (-\sin(\omega t - c)) &= -\omega \cos(\omega t - c) \\ \frac{d}{dt} \sin\left(\frac{2}{3}\omega t\right)^2 &= \frac{8}{9}\omega^2 t \left(\cos \frac{4}{9}\omega^2 t^2\right) \\ \frac{d}{dt} \sin^2 t + 2 \cos^2 t &= 2 \sin t \cos t + 2 \cos^2 t\end{aligned}$$

$$\begin{aligned}\frac{d}{dt} 2 \sin \omega_1 t \cdot \cos \omega_2 t &= \frac{d}{dt} 2 \sin \omega_1 t \cdot \cos \omega_2 t \\ \frac{d}{dt} (2 \sin \omega_1 t \cdot \cos \omega_2 t)^2 &= 8 (\sin \omega_1 t \cos^2 \omega_2 t \cos \omega_1 t) \omega_1 - 8 (\cos \omega_2 t \sin \omega_2 t) \omega_2 + 8 (\cos \omega_2 t \sin \omega_2 t) \omega_2 \cos^2 \omega_1 t \\ \frac{d}{dt} \sqrt[3]{\sin\left(\frac{2}{3}\omega t\right)^2} &= \frac{8}{27} \frac{\sqrt[3]{\sin \frac{4}{9}\omega^2 t^2}}{\sin \frac{4}{9}\omega^2 t^2} \left(\cos \frac{4}{9}\omega^2 t^2\right) \omega^2 t\end{aligned}$$

$$\frac{d}{dt} \frac{U}{\sin 2\omega t} = -2U (\cos 2\omega t) \frac{\omega}{1 - \cos^2 2\omega t} \quad (1)$$

$$\frac{d}{dt} \sin \frac{5}{t} = -5 \frac{\cos \frac{5}{t}}{t^2} \quad (2)$$

$$\frac{d}{dt} (\sin \cos \omega t)^2 = -2\omega \sin(\cos \omega t) \cos(\cos \omega t) \sin \omega t \quad (3)$$

$$\frac{d}{dt} \tan 5t = 5 + 5 \tan^2 5t \quad (4)$$

$$\frac{d}{dt} e^{\sin^2 2\omega t} = 4\omega (\sin 2\omega t \cos 2\omega t) e^{-(\cos 2\omega t - 1)(\cos 2\omega t + 1)} \quad (5)$$

3. Finde Stammfunktion bzw. berechne das Integral

$$\begin{aligned}\int \sin 2\omega t dt &= -\frac{1}{2\omega} \cos 2\omega t + C \\ \int \sin 3(-2\omega t) dt &= \frac{1}{6\omega} \cos 6\omega t + C \\ \int (\sin 2\omega t + \cos \omega t) dt &= -\frac{1}{2\omega} \cos 2\omega t + \frac{\sin \omega t}{\omega} + C \\ \int_0^{\frac{\pi}{2}} \cos \frac{1}{2}\omega t dt &= 2 \frac{\sin \frac{1}{4}\omega T}{\omega} = \frac{1}{\pi} T \\ \int_0^T \sin 2\omega t dt &= -\frac{1}{2} \frac{\cos 2\omega T - 1}{\omega} \quad \text{mit } \omega = \frac{2\pi}{T} \text{ dann } 0 \\ \int_0^{\frac{\pi}{4}} \cos \omega t dt &= \frac{\sin \frac{1}{4}\omega T}{\omega} = \frac{1}{2\pi} T \\ \int_0^{3T} |\sin \omega t| dt &= 6 \int_0^{\frac{\pi}{2}} \sin \omega t dt = -6 \frac{\cos \frac{1}{2}\omega T - 1}{\omega} \quad \text{mit } \omega = \frac{2\pi}{T} \text{ dann } \frac{6}{\pi} T\end{aligned}$$